



# Evolution of mass determination in Pluto's system

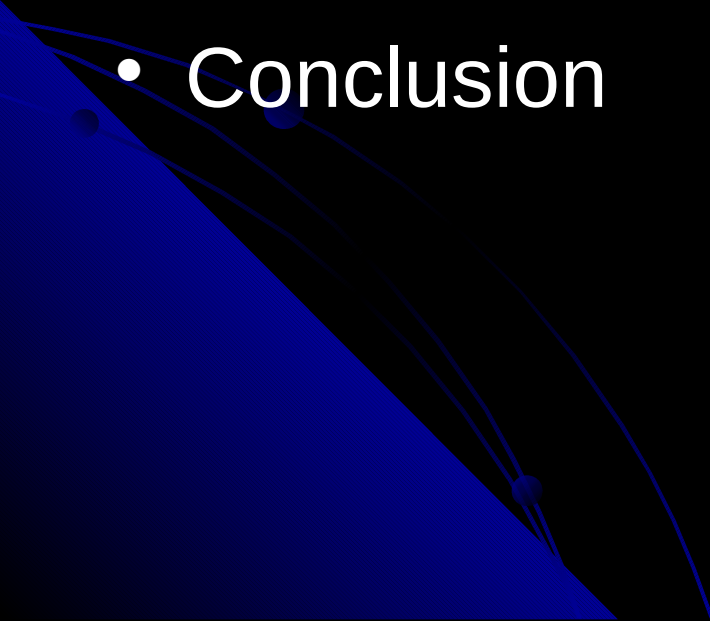
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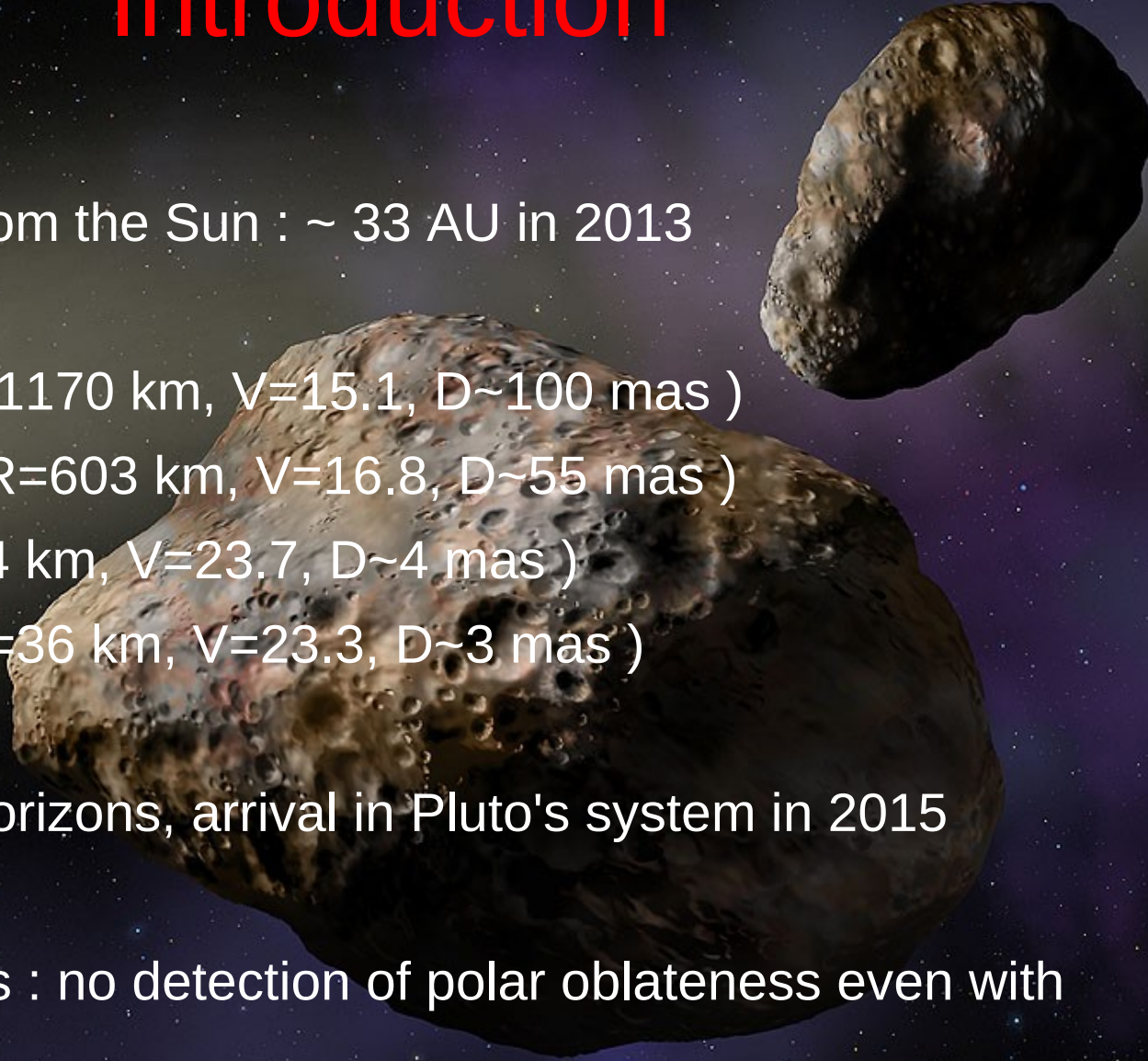
GAIA Solar System Science - Pisa 2011

# Plan

- Introduction
  - Dynamical Model
  - Data simulation
  - Results
  - Conclusion
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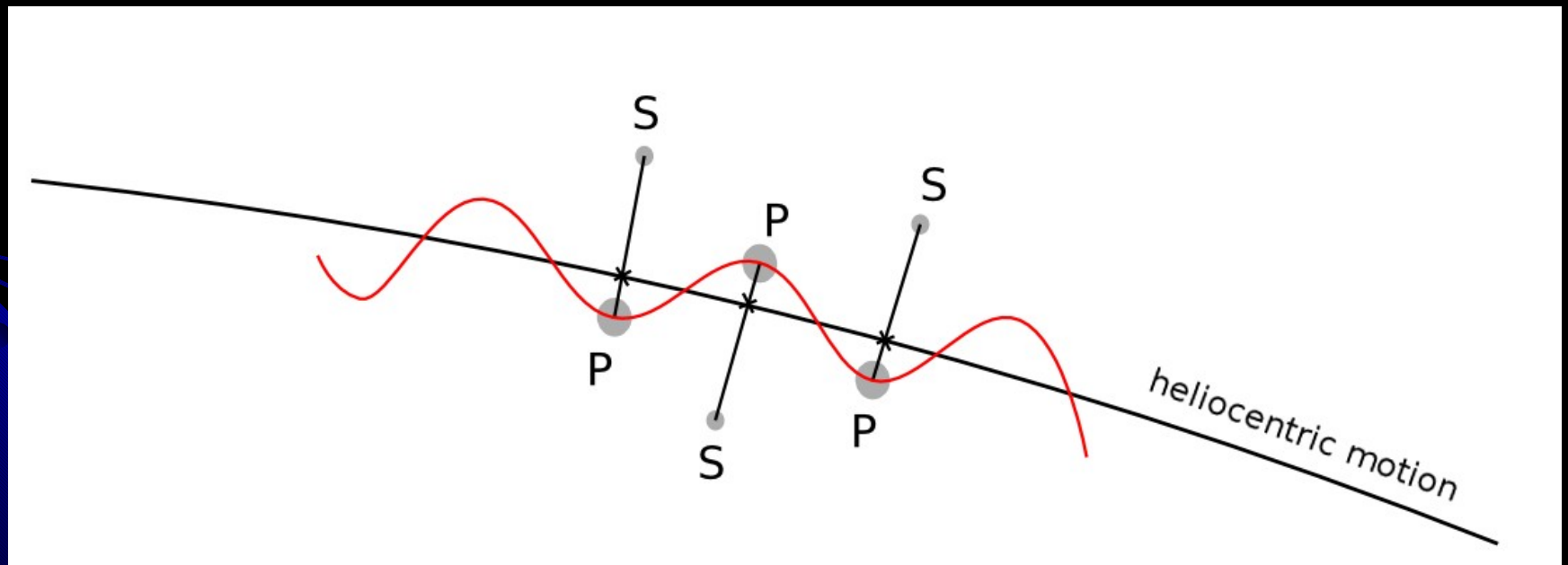


# Introduction

- Pluto's system :
    - Distance from the Sun :  $\sim 33$  AU in 2013
    - 4 objects :
      - Pluto (R=1170 km, V=15.1, D $\sim$ 100 mas )
      - Charon (R=603 km, V=16.8, D $\sim$ 55 mas )
      - Nix (R=44 km, V=23.7, D $\sim$ 4 mas )
      - Hydra (R=36 km, V=23.3, D $\sim$ 3 mas )
  - Mission New Horizons, arrival in Pluto's system in 2015
  - Previous results : no detection of polar oblateness even with New Horizons
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# Dynamical model

- Binary object → center of mass not within the primary  
Coupling between heliocentric motion of the primary and orbital motion of the satellites



→ solution : fitting the motion of every object around the Sun

- Numerical integration of four objects' motion around the Sun
- Planetary and Sun perturbations using DE406
- Initial conditions and masses from DE406 and Tholen (2008)
- No spherical harmonics included

$$\ddot{\vec{r}}_i = \sum_{j=1}^{\mathcal{N}} -\frac{GM_j(\vec{r}_i - \vec{r}_j)}{r_{ij}^3} + \sum_{l=1, l \neq i}^4 -\frac{Gm_l(\vec{r}_i - \vec{r}_l)}{r_{il}^3}$$

# Data simulation

- Goal : estimate the uncertainty we will obtain with a set of observations
- Method :
  - Simulation of observations according to the tested schedule
  - Fitting of the model to the simulations, fitted parameters : initial positions and velocities, and masses
  - Extraction of the  $1\text{-}\sigma$  uncertainty from the least-square procedure

- Schedules used :
  - Currently available observations of the satellites (Buie 2006, Weaver et al. 2005, Sicardy et al. 2006, Tholen 1997)
  - Simulation of future observations between 2010 and 2014, 10 per year
  - New Horizons schedule and uncertainty
  - GAIA schedule simulation
- New Horizons : short period observations, varying precision with the distance of the probe, observations of the four objects of the system
- GAIA : observations simulated from 2013 to 2017, 1 mas constant precision, only Pluto and Charon observed

# Center of mass determination



- Center of mass determination at best at  $1/8$  of Nix's and Hydra's diameter



# Results

set of simulated observations	1- $\sigma$ error bars on the masses ( $\text{km}^3\text{s}^{-2}$ )			
	Pluto	Charon	Nix	Hydra
1992-2006	1.28	0.51	0.024	0.036
		72	16	17
1992-2014	0.82	0.28	0.010	0.019
		125	68	69
1992-2006+NH	0.27	0.072	0.012	0.0028
		129	106	124
1992-2014+NH	0.25	0.045	0.0076	0.0026
		181	158	176
1992-2014+extended NH	0.19	0.039	0.0070	0.0024
		181	186	233
1992-2014+NH+GAIA	0.17	0.017	0.0054	0.0024
		66	247	158

1- $\sigma$  error bars on the masses given by least square method using different sets of simulated observations, with  $m_1 = 870.3 \text{ km}^3\text{s}^{-2}$ ,  $m_2 = 101.4 \text{ km}^3\text{s}^{-2}$ ,  $m_3 = 0.039 \text{ km}^3\text{s}^{-2}$  and  $m_4 = 0.021 \text{ km}^3\text{s}^{-2}$ .

# Orbit enhancement thanks to GAIA before New Horizons arrival

set of simulated observations	1- $\sigma$ error bars on the masses ( $\text{km}^3 \cdot \text{s}^{-2}$ )			
	number of simulated observations			
	Pluto	Charon	Nix	Hydra
2002-2013	0.95	0.24	0.010	0.022
		125	68	69
2002-2013+GAIA before 2015	0.45	0.035	0.0086	0.016
	41	166	68	69

set of simulated observations	1- $\sigma$ error bars on the semi-major axis (km)		
	Charon	Nix	Hydra
2002-2013	5.8	23	155
2002-2013+GAIA before 2015	3.25	10	43

# Fitting to real observations

- Problem : scale unconstitancy between the different HST sets → uncertainties increasing
- Uncertainty on the masses greater than in our previous study



# Fitting to real observations

	Charon		Nix		Hydra	
	$\Delta RA$	$\Delta Dec$	$\Delta RA$	$\Delta Dec$	$\Delta RA$	$\Delta Dec$
Mean value of the residuals (mas)	1.1	0.12	-5.2	-2.5	0.8	3.0
Standard deviation of the residuals (mas)	5.8	3.9	18.3	16.5	11.4	9.0

Table 1 : statistics of the post-fit residuals for Pluto's satellites

	Pluton	Charon	Nix	Hydra
GM ( $\text{km}^3 \cdot \text{s}^{-2}$ )	$872.8 \pm 1.8$	$100.6 \pm 0.3$	$0.046 \pm 0.026$	$0.011 \pm 0.036$

Table 2 : fitted masses and errors for Pluto and its satellites

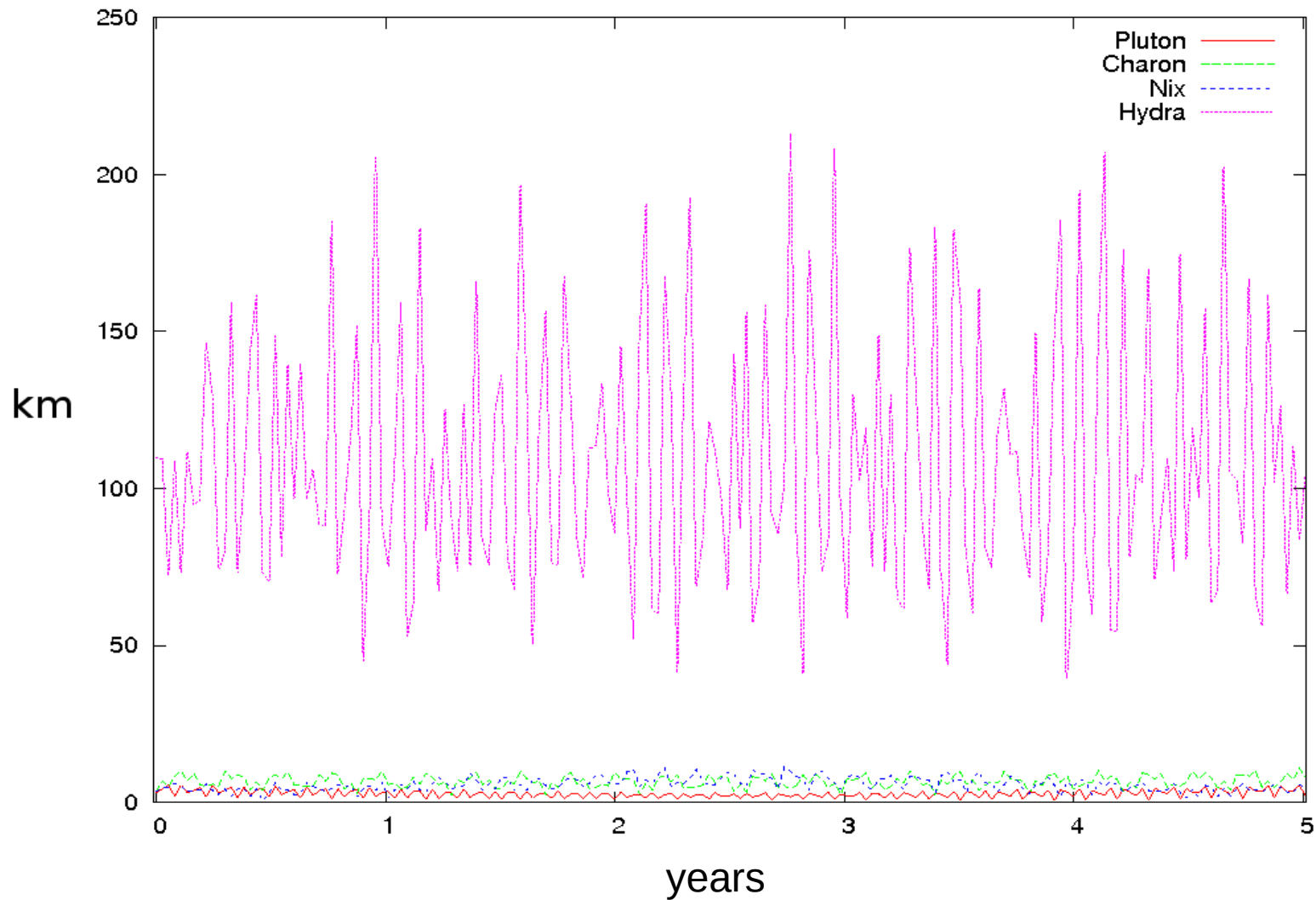
# Conclusion

- Precise mass determination will have to wait for New Horizons
- GAIA will be able to improve the orbit of Pluto's satellites, even before New Horizons arrival
- GAIA will improve the uncertainties on the system's masses
- Though GAIA does not observe Nix and Hydra, the constraints put on Pluto and Charon are expected to lower the uncertainties on Nix's and Hydra's dynamical parameters

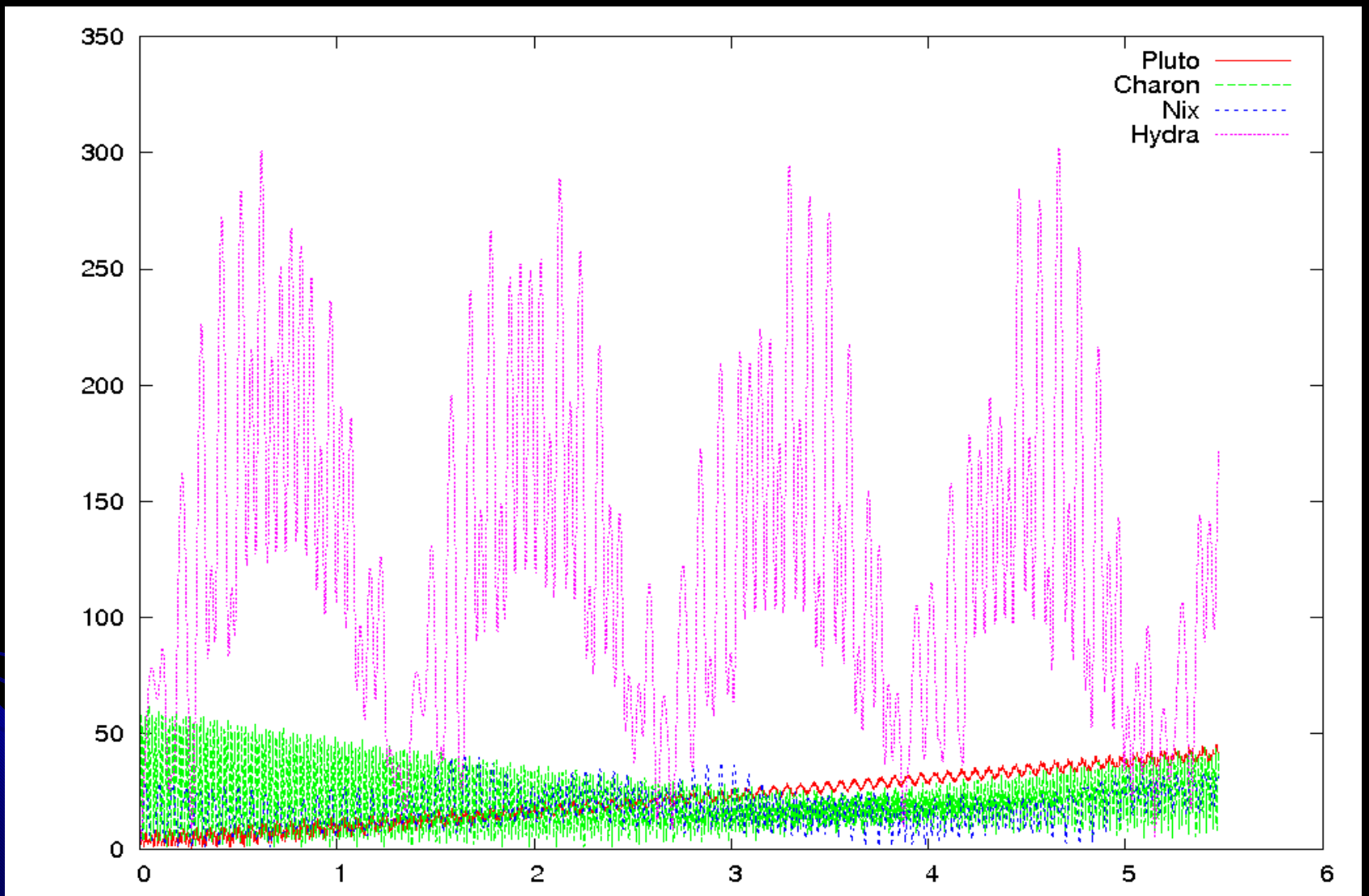


# Why constraining Pluto and Charon helps ?

- What influences Nix's and Hydra's orbit :
  - Masses
  - Positions of Pluto and Charon
- When adjusting the orbit, the residuals are reduced by adjusting parameters
- If a parameter which has a strong influence on Pluto and Charon motion is fixed, it can no longer absorb the residuals
  - constraining Pluto's and Charon's dynamical parameters means higher residuals on Nix and Hydra
  - clearer effect of their dynamical parameters
  - higher precision on these parameters



Post-fit residuals of a model with a massless Nix fitted to simulated observations with  $GM_{\text{Nix}} = 0.039 \pm 0.034 \text{ km}^3 \cdot \text{s}^{-2}$



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