

Search for spacetime anisotropy with the MICROSCOPE mission

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Testing Lorentz symmetry

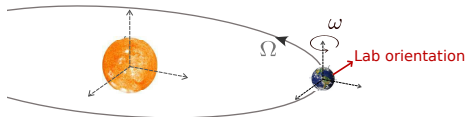
Local Lorentz Invariance

The outcome of an experiment is independent of the boost and orientation changes

- Observer invariance - invariance under coordinate changes
- Particle invariance - invariance under rotations and boost performed in a given observer frame

Lorentz symmetry breaking : spacetime anisotropy

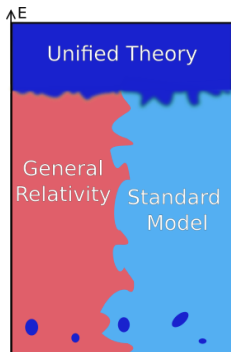
- Observer invariance holds
- Particle invariance is violated



Standard Model Extension (SME) framework

What is SME?

- Effective field theory built from SM fields & in curved spacetime
- General framework describing low-energy effects of a spontaneous Lorentz violation (LV) occurring at Planck scale



Main features

- Includes all possible observer-independent LV built from SM fields and background coefficients in the Lagrangian
- These coefficients vanish if the symmetry is preserved
- LV terms are expected to be strongly suppressed compared with non violating terms
- Phenomenological, not quantitatively predictive
- Enables the derivation of experimental observables

[Kostelecky *et al.*, PRD 51, 1995], [Kostelecky *et al.*, PRD 58, 1998]

Characteristic

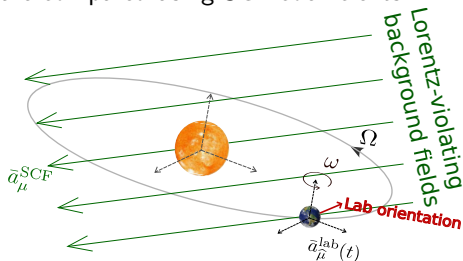
- Lorentz violations arise from interaction with LV background coefficients
- Amplitude of deviations parametrized by SME background coefficients

About SME coefficients and violation signals

- SME coefficients are coordinate dependent
- In the lab frame coefficients are time dependent, leading to time dependent observables
- They are assumed to be constant in a cosmological frame and therefore in the SCF over the timescale of the experiment
- By convention all experiments are compared using SCF coefficients

$$c_{ij}^{\text{lab}}(t) \xrightarrow{T} c_{IJ}^{\text{SCF}}$$

(coordinate transformation from lab frame to an inertial frame)



LLI violation signals in the SME

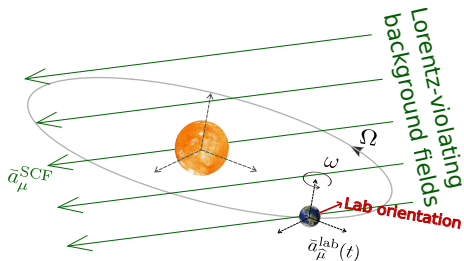
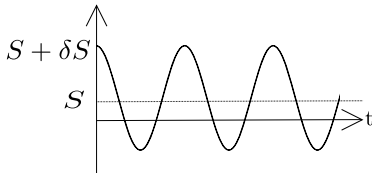
Lab frame observable:

$$\delta S(t, \vec{x}) = f(\vec{a}_i^{\text{lab}}(t))$$

Sun Centered Frame (SCF) observable:

$$\delta S(t, \vec{x}) = \sum_n A_n (\vec{a}_i^{\text{SCF}}) \cos(\omega_n t) + B_n (\vec{a}_i^{\text{SCF}}) \sin(\omega_n t)$$

Observable S in SCF



SME model for MICROSCOPE

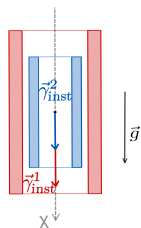
Standard WEP :

$$2\vec{\gamma}^{(d)} = \delta\vec{g} + ([T] - [In])\vec{\Delta} - 2[\Omega]\dot{\vec{\Delta}} - \ddot{\vec{\Delta}}$$

SME WEP:

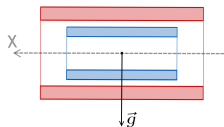
$$2\vec{\gamma}^{(d)} = \underbrace{A \Delta \vec{a}_t^{\text{GCRF}}}_{\text{SME equivalent to } \delta} \vec{g} + ([T] - [In])\vec{\Delta} - 2[\Omega]\dot{\vec{\Delta}} - \ddot{\vec{\Delta}} - \underbrace{\left[\frac{B}{5cr^5} R^T \vec{r} (\vec{\omega} \wedge \vec{r})^k \Delta \vec{a}_k^{\text{GCRF}} + \frac{C}{5cr^3} R^T \vec{\nabla} (\vec{\omega} \wedge \vec{r})^k \Delta \vec{a}_k^{\text{GCRF}} \right]}_{\text{Analogous to a gravitomagnetic term}}$$

”Standard” WEP violation

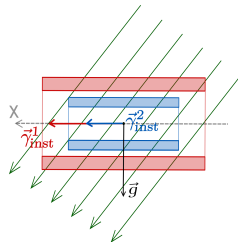


Signal $\neq 0$

”SME” WEP violation



No signal



Signal $\neq 0$

SME observable with SCF coefficients

$$2\vec{\gamma}^{(d)} = 2 \left(\Delta \vec{a}_T^{\text{SCF}} + \frac{\dot{x}_\oplus}{c} \Delta \vec{a}_x^{\text{SCF}} + \frac{\dot{y}_\oplus}{c} \Delta \vec{a}_y^{\text{SCF}} + \frac{\dot{z}_\oplus}{c} \Delta \vec{a}_z^{\text{SCF}} \right) \vec{g} + ([T] - [In]) \vec{\Delta} - 2[\Omega] \dot{\vec{\Delta}} - \ddot{\vec{\Delta}} \\ - \frac{6GMR_\oplus^2}{5cr^5} R^T \vec{r} (\vec{\omega} \wedge \vec{r})^k \Delta a_k^{\text{SCF}} + \frac{2GMR_\oplus^2}{5cr^3} R^T \vec{\nabla} (\vec{\omega} \wedge \vec{r})^k \Delta a_k^{\text{SCF}}$$

- Acceleration Tsage : 3 differential accelerations & time scale
- SME model parameters
- Earth's boost components (INPOP)
- Gravity file : 3 acceleration & 6 gradients
- Angular velocity (3) and acceleration (3)
- Attitude file : 4 components of quaternions
- Orbito file : 3 positions

Lorentz invariance vs "standard" WEP test

Frequencies

Suppression	SME coefficients	Frequency
1	$\Delta \bar{a}_{\tilde{Y}}^{\text{SCF}}$	ω_{ep}
10^{-4}	$\Delta \bar{a}_{\tilde{X}, \tilde{Y}}^{\text{SCF}}$	$\omega_{\text{ep}} \pm \Omega$
10^{-6}	$\Delta \bar{a}_{\tilde{Z}}^{\text{SCF}}$	$\omega_{\text{ep}} \pm \Omega$
10^{-6}	$\Delta \bar{a}_{\tilde{X}, \tilde{Y}}^{\text{SCF}}$	$\omega_{\text{ep}} \pm (\omega_{\text{orb}} \pm \Omega)$
		$\omega_{\text{spin}} \pm \Omega$

Main limitations - test masses offcenterings Δ

- Offcenterings could mimic LV signals due to gravity gradient
- Fitted as parameters of the analysis
- Investigate correlations between SME coefficients and offcenterings

First SME model [Kostelecky and Tasson, PRD 83, 2011]

SME Microscope proposal (SYRTE, LKB, J. Tasson, Q. Bailey) in 2015

Lorentz violating coefficients

- $\bar{c}_{\mu\nu}$ and \bar{a}_{μ} lead to composition dependent trajectories of the test masses
- $\bar{c}_{\mu\nu}$ have already been strongly constrained with clocks
- Potential improvement by up to 3 orders of magnitude on several \bar{a}_{μ} coefficients depending on the noise and systematics

Status

SME model

- ✓ Analytical derivation of the instrument observable in terms of GCRF violating coefficients and in-flight parameters
- ✓ Same thing for the instrument observable in terms of SCF coefficients
 - Transformation from GCRF to SCF coefficients using INPOP ephemerides for Earth's position and boost

Data analysis

- Toy-model adjustment on simulated data provided by OCA/ONERA
 - ✓ Without noise (least-squares) : no WEP violation, offcenterings $\Delta_x = 20\mu m$ and $\Delta_z = 20\mu m$
 - With a realistic noise and a noise model (MC simulations - **On going**)
 - Blind tests on simulated data with/without WEP violation and offcenterings, with a realistic noise and gaps
- Full SME test on real data

Thank you for your attention!

Thanks to Gilles Métris for providing simulated data and related documentation