



**Influence of the data process in the
determination of the Equivalence Principle
violation signal for the MICROSCOPE
experiment**

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r e t o u r s u r i n n o v a t i o n

The Equivalence Principle

PE → **Universality of free fall** :
all bodies, independently of their
mass or intrinsic composition,
acquire the same acceleration in
the same uniform gravity field

$$\frac{M_G}{M_I} = 1$$

Quantum Mechanics, Standard model:
electromagnetic, strong, weak
interaction

≠ Geometrical theory of the gravitation

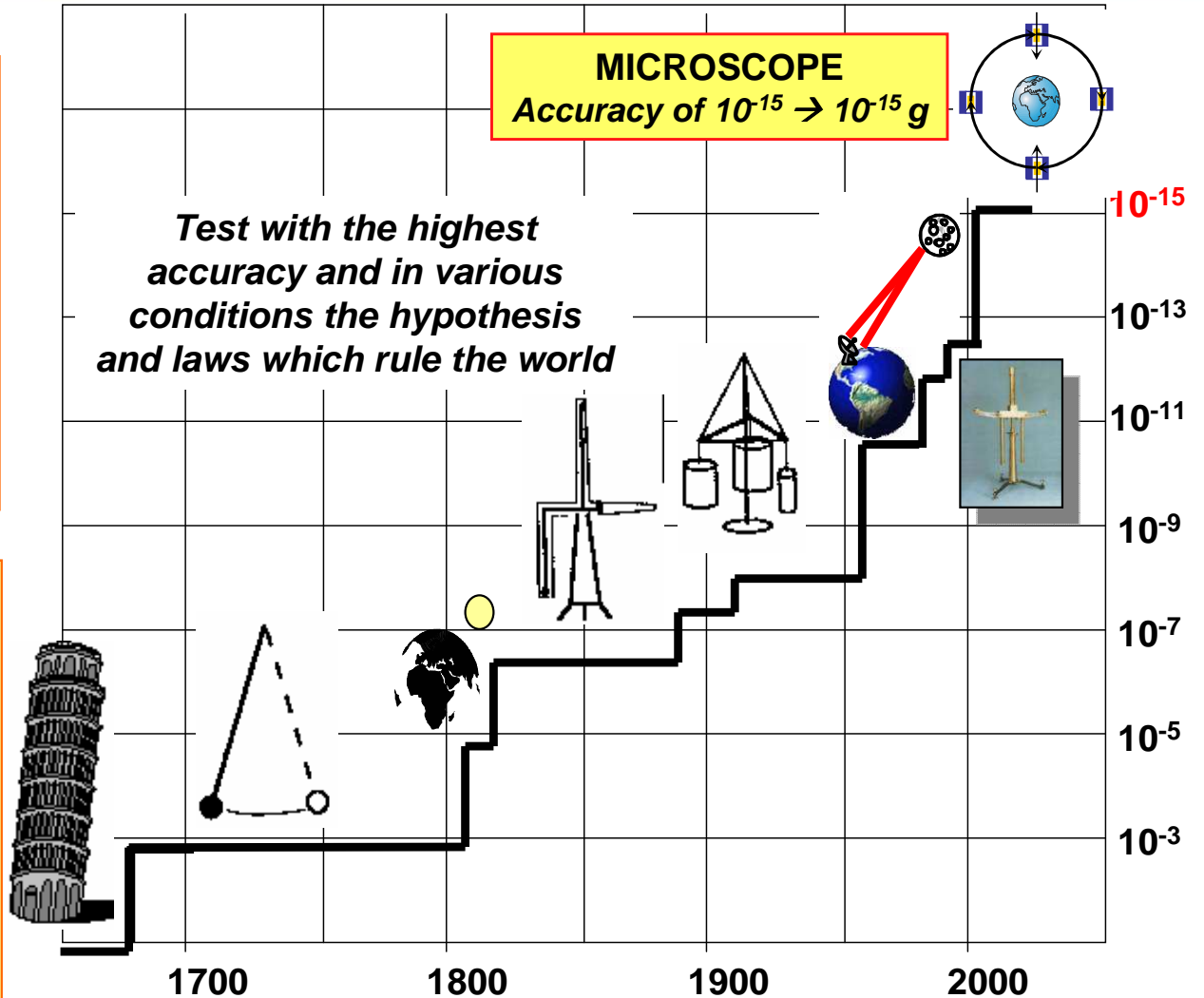
Super-symmetry: Sparticules, LHC

String theory, Branes...

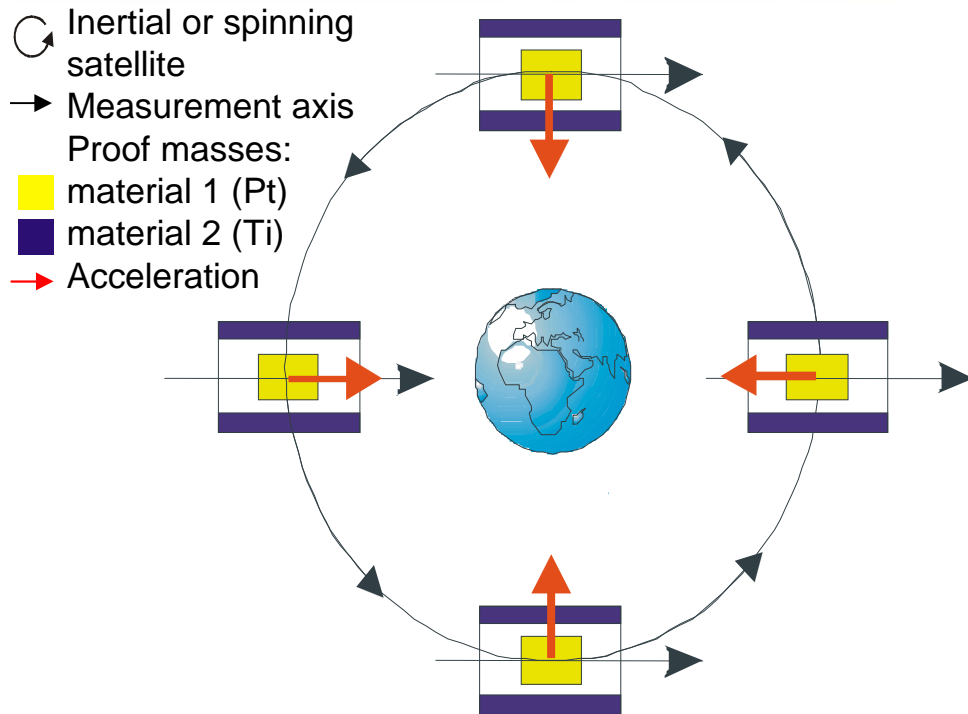
⇒ New interaction?

⇒ Violation of the Equivalence
principle?

$$\frac{M_G}{M_I} = 1 + \omega$$



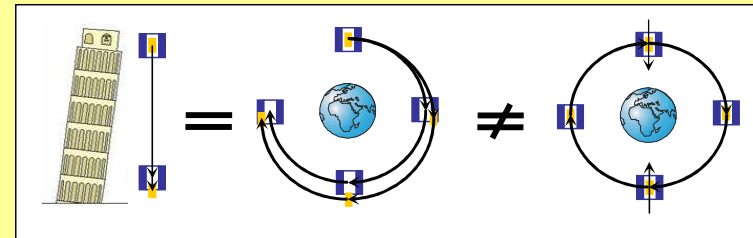
The principle of the MICROSCOPE space mission



CNES MYRIADE Microsatellite

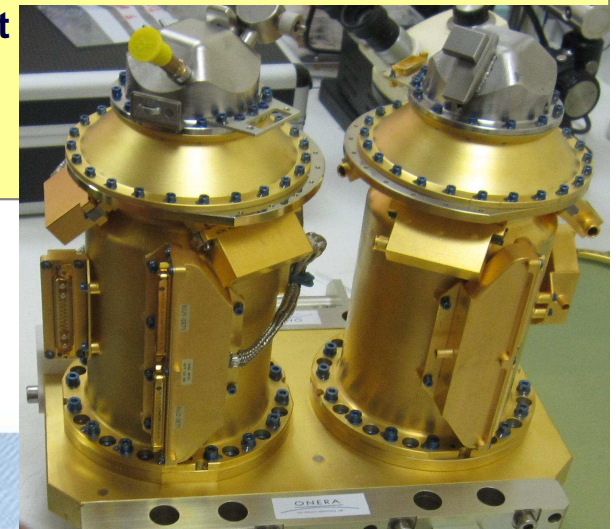
- Circular Orbit: 720 km, $e < 5 \cdot 10^{-3}$
- Inertial or Rotating: $7 \cdot 10^{-3}$ rd/s
- Mission duration: 12 months
- Mass of microsat: 200 kg
- Payload budgets: 35 kg, 40 Watts
- 2 differential electrostatic accelerometers (2 pairs of masses: Pt/Pt & Pt/Ti)

- Gravitational source: **the Earth**
- inertial acceleration: orbital motion
- 2 masses of **different composition**: controlled **on the same orbit** ($< 10^{-11}$ m) thanks to the measured electrostatic forces

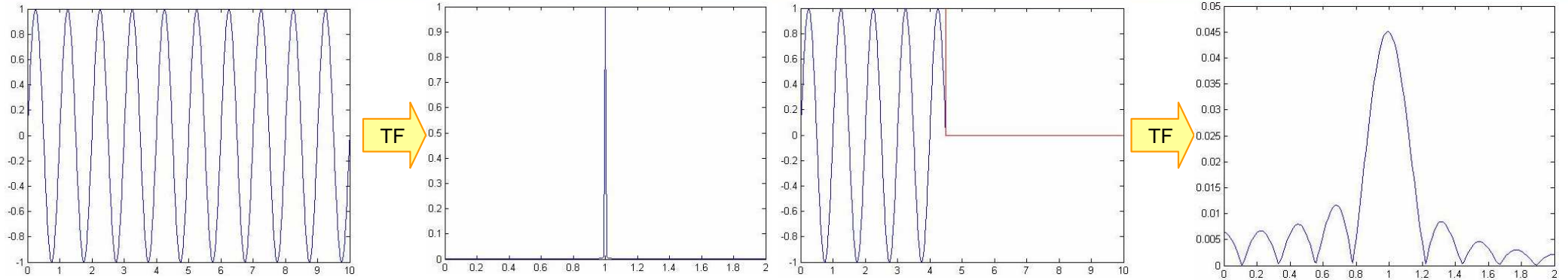


- time span of the measurement: **non limited by the free fall** (> 20 orbits)
- Environment: Very controlled or avoiding perturbations, **drag-free satellite**
- Signal to be detected: phases & frequency are defined $f_{ep} =$

- **Inertial mode:** $f_{orb} = 1/orbit$
- **Spinning mode:** $f_{orb} + f_{spin}$



Influence of the observation window



- Aliasing: a perturbation at any frequency has a component at the EP violation frequency (f_{EP})

Projection rate of a perturbation on the EP violation signal at f_{EP} :

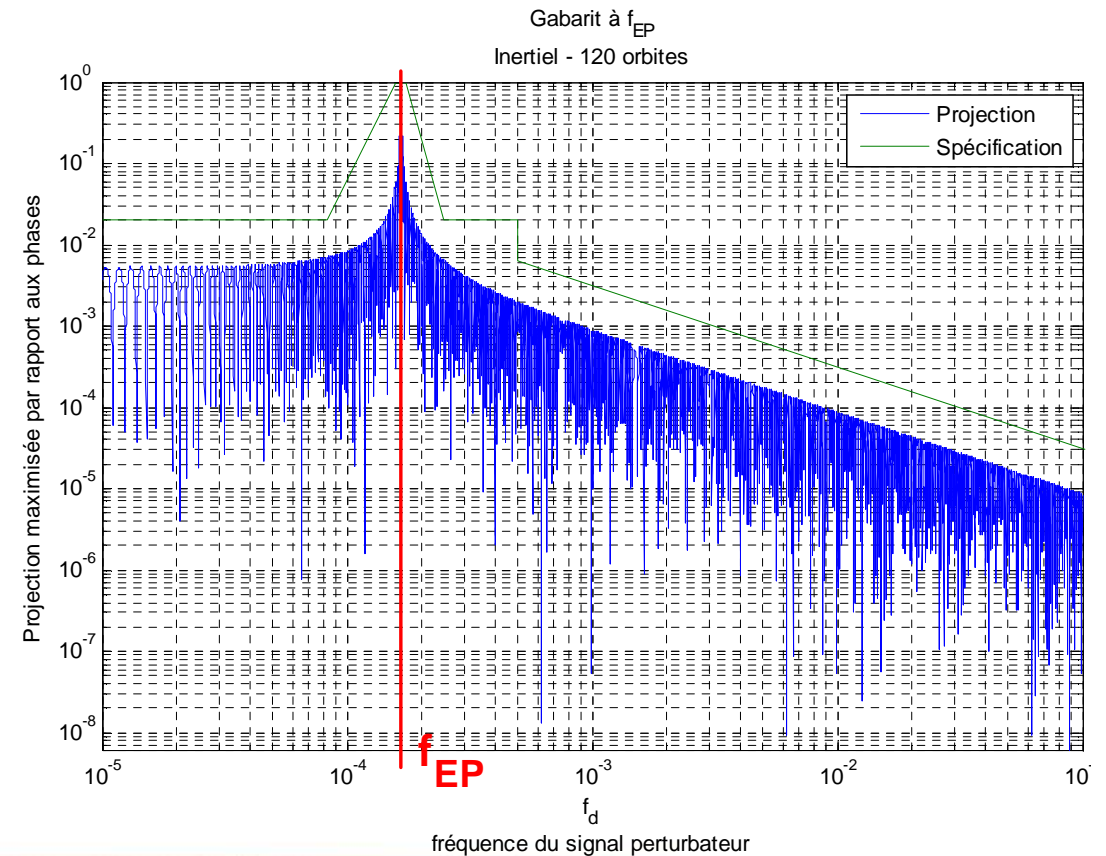
EP violation signal:

$$S_{EP} = A_{EP} \sin(\omega_{EP}t + \varphi_{EP})$$

Disturbance signal:

$$S_d = A_d \sin(\omega_d t + \varphi_d)$$

$$\tau = \frac{\langle S_{EP}, S_d \rangle}{\langle S_{EP}, S_{EP} \rangle}$$



Choice of the measurement duration and spin frequency

Main disturbance: due to the orbital or spin motion

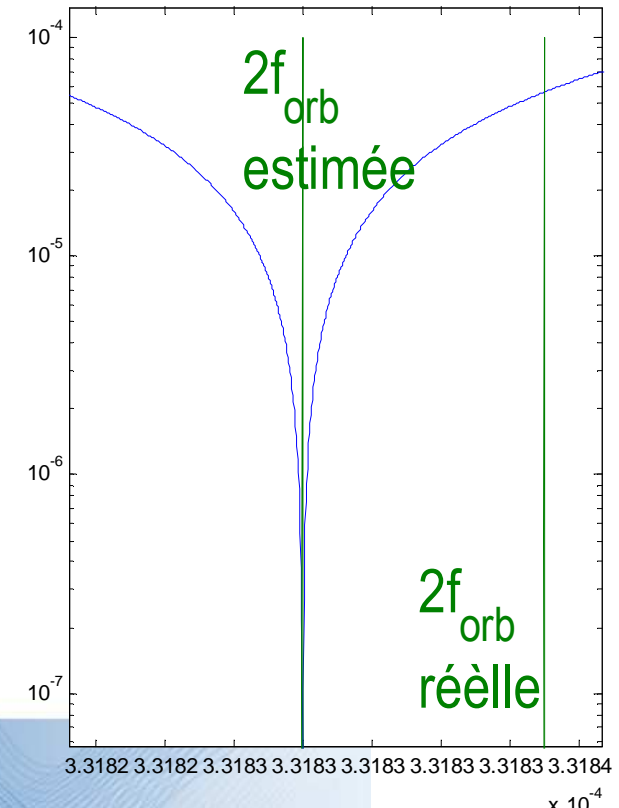
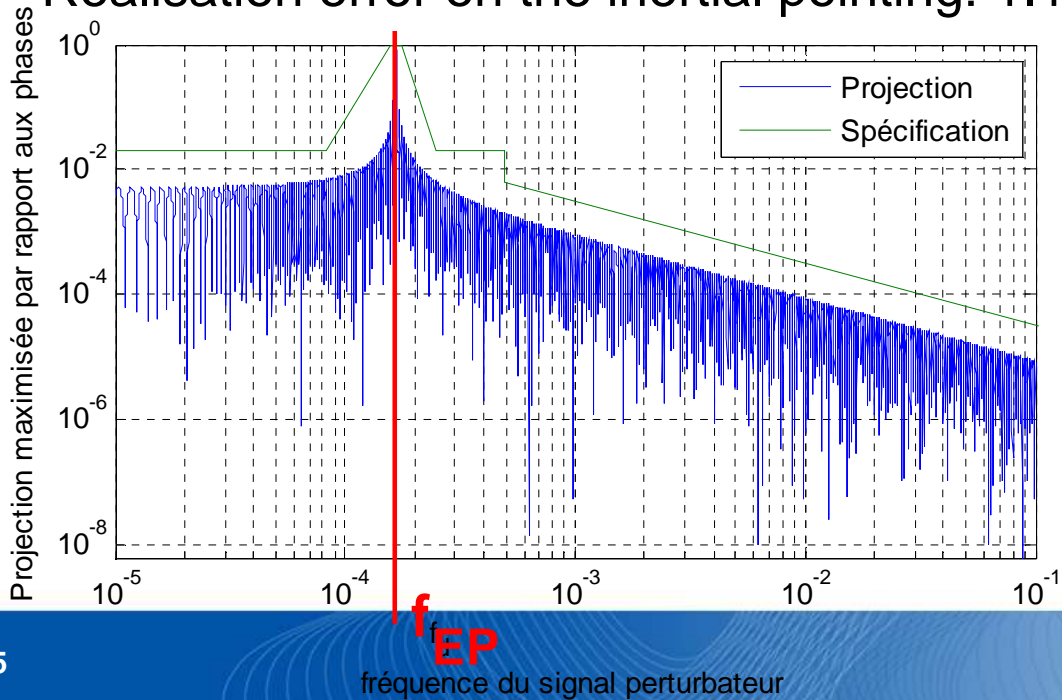
→ choice of f_{spin} and $T_{\text{observation}}$ to have minimal projection rates:

- $T_{\text{observation}} = k_1 \cdot T_{\text{orb}}$
- $T_{\text{observation}} = k_2 \cdot T_{\text{spin}}$

Inertial mode	Spinning mode	
$k_1 = 120$	$k_1 = 20$	to reduce the noise
	$k_2 = 73$	

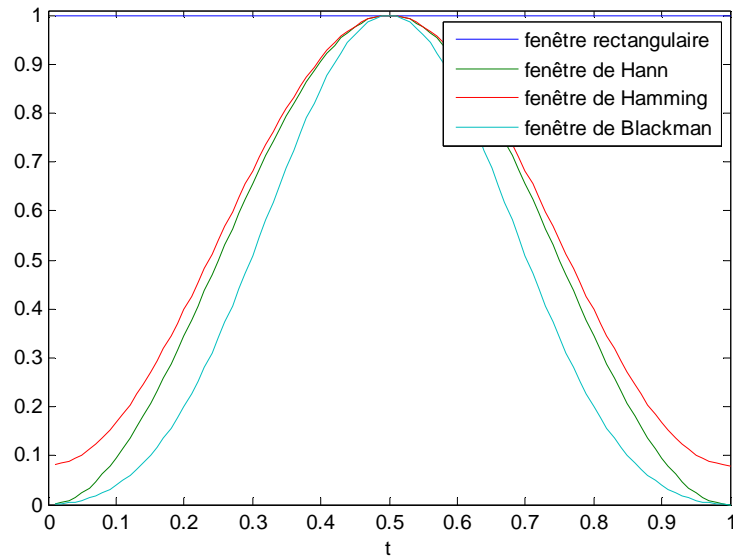
Influence of the incertitude and realisation error:

- Incertitude on the orbital frequency : $2 \cdot 10^{-8} \text{rad/s}$ (\leftrightarrow 100m for the orbit altitude)
- Command error on the spin frequency: $3 \cdot 10^{-8} \text{rad/s}$
- Realisation error on the inertial pointing: $1 \cdot 10^{-8} \text{rad/s}$

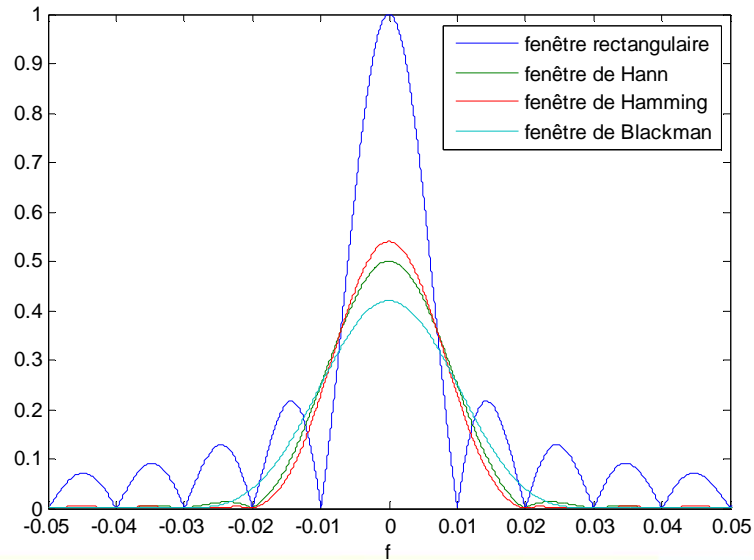


Non-rectangular windows

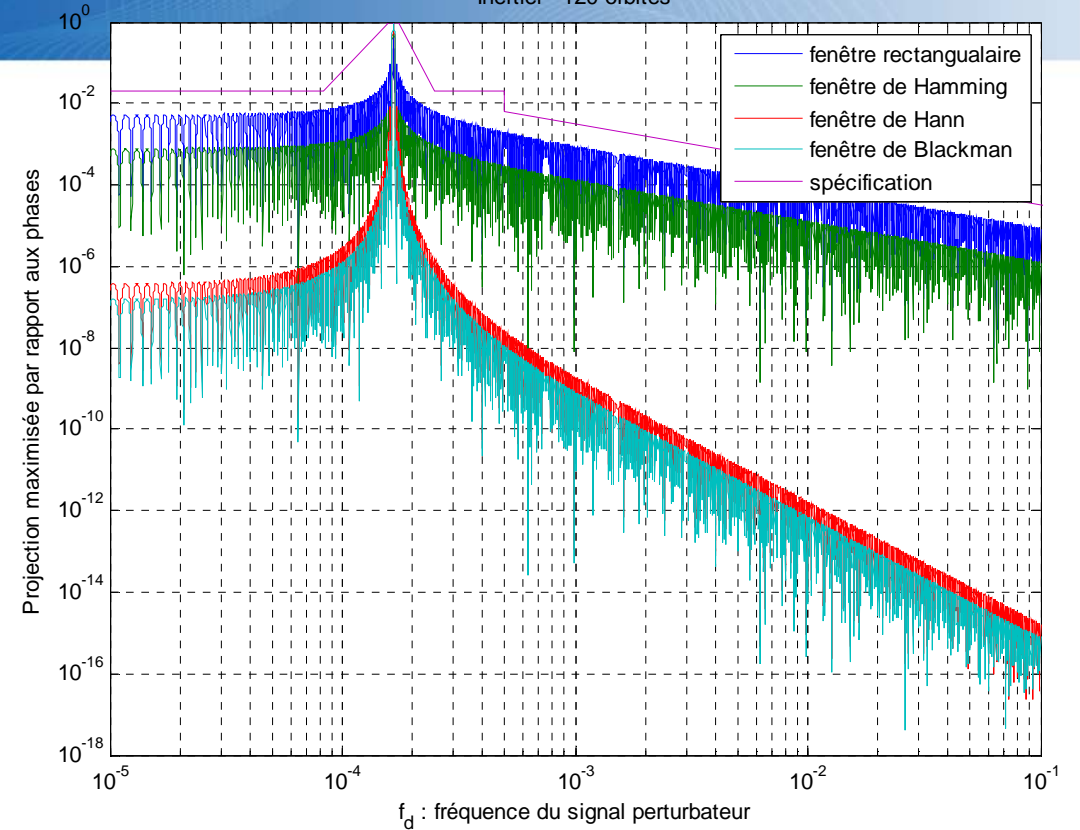
Fenêtres temporelles



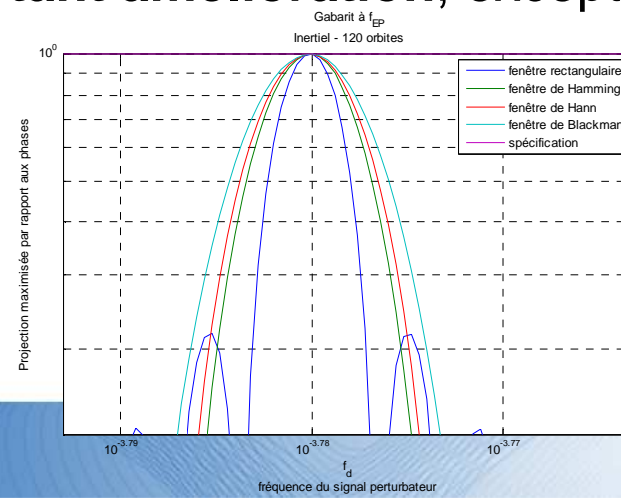
Transformée de Fourier des fenêtres



Gabarit à f_{EP}
Inertiel - 120 orbites



Comparison between different windows:
important amelioration, except around f_{EP}



Measurement losses

- **Teletransmission errors**

Information from the Picard mission:

- **frequency:** about 100 events in 10 months
- **duration:** seconds - hours

- **Coating crackings**

- due to the temperature changes (Earth / Space vacuum)
- **frequency:** for each of the four satellite sides, about 6 times when facing the Earth
- **duration:** 0.5-0.75s → 2 or 3 measurement points

- **Tank crackings**

- worst case, depending of the gas pressure
- **frequency:** for each of the 6 tanks, about 43 times/orbit
- **duration:** 0.5s → 2 measurement points

Measurement losses

- Without measurement losses:

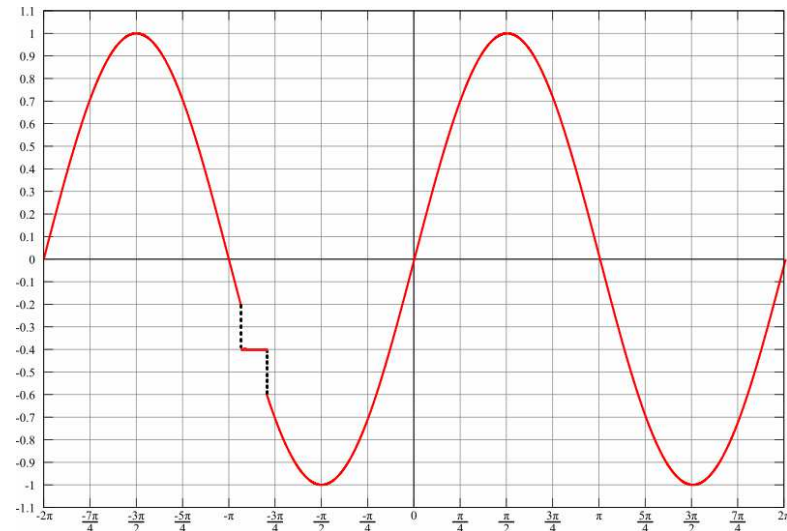
$$TF(S) = TF(\text{sin wave}) * TF(\text{rect pulse})$$

- With measurement losses: replacement by zeros

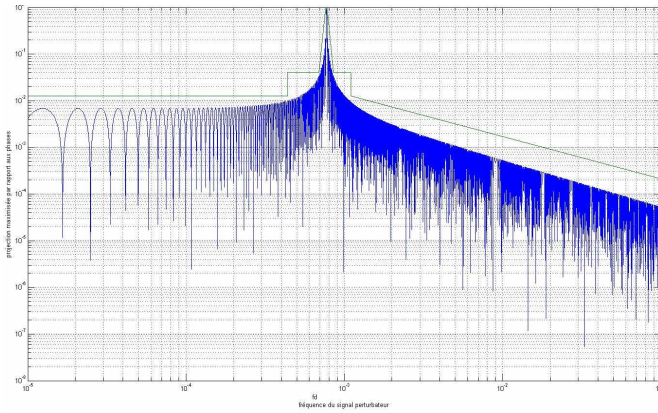
$$TF(S) = TF(\text{sin wave}) * TF(\text{rect pulse with zero gap})$$

- With measurement losses: replacement by the mean value of the measurement before and after the interruption

$$TF(S) = TF(\text{sin wave}) * TF(\text{rect pulse with mean value gap})$$

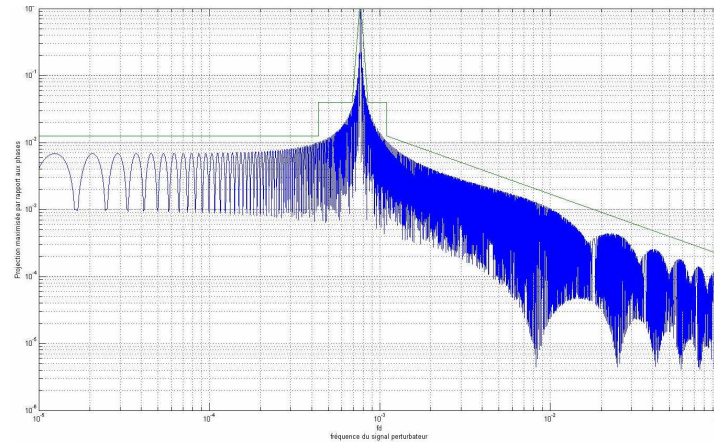


Short duration loss



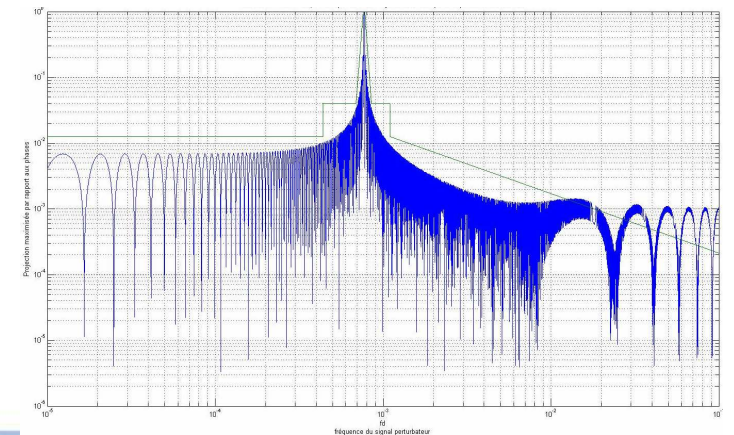
- one measurement loss
- simulations with different duration
- respect the specifications up to 1 minute

No measurement loss



First method:
replacement by zeros

Second method: replacement
by the mean value before and
after the interruption



Division in subsections

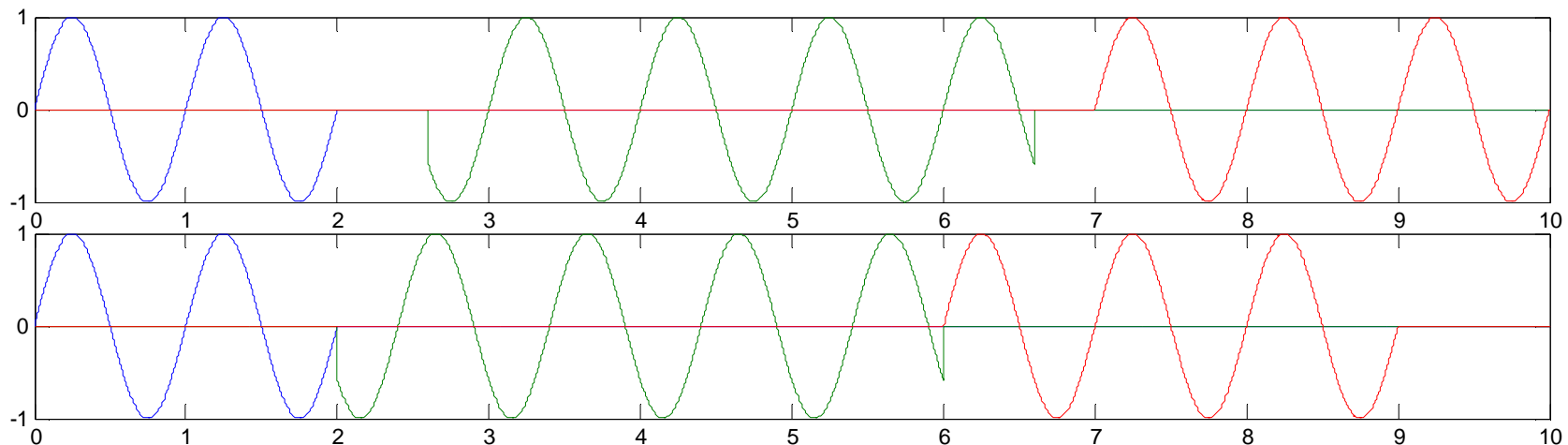
Success criterium: maximal one measurement loss of duration < 1 minute per session

Activity	Probability of failure
Spinning session: 20 orbits	2,9%
Inertial session: 120 orbits	16%

For data losses > 1 minute in inertial session:

→ inertial session of 120 orbits divided in **several subsections**

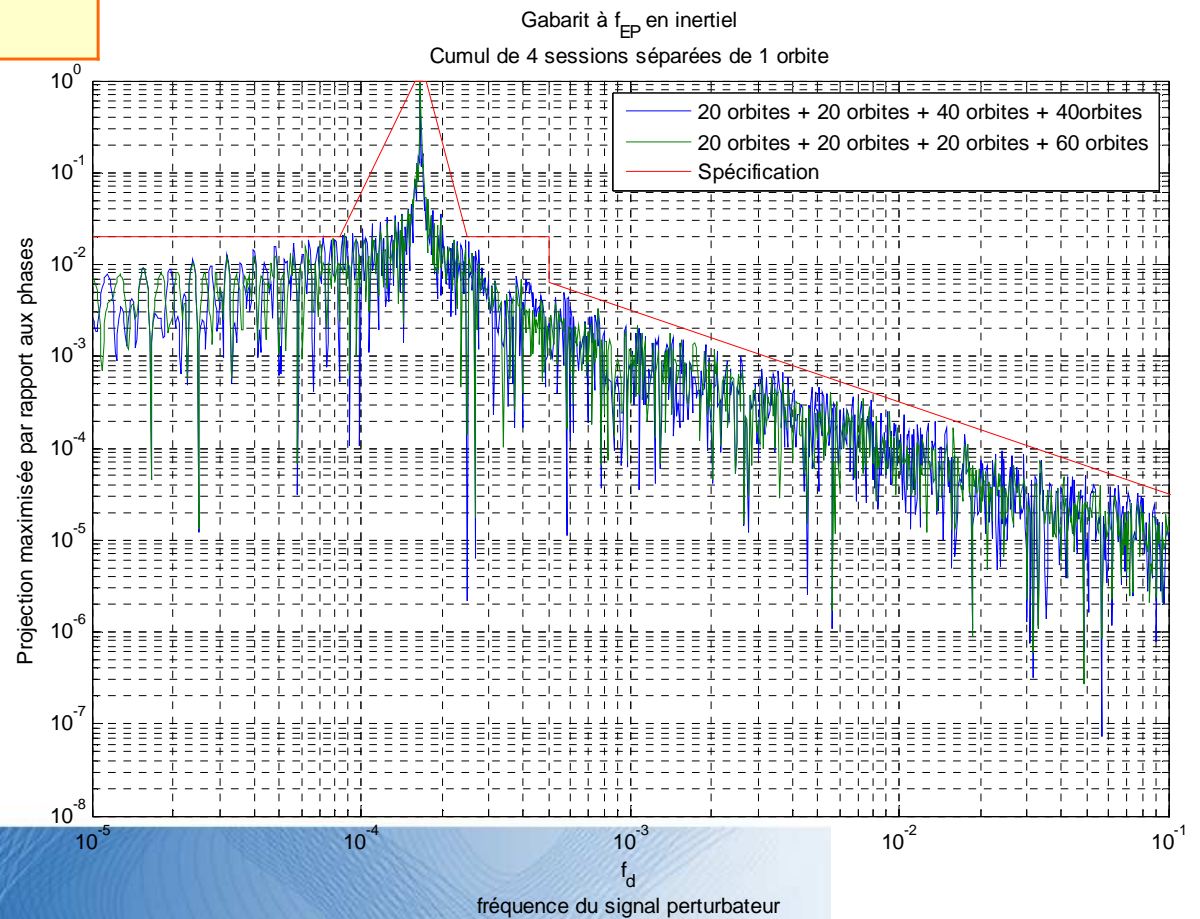
- $T_{\text{subsection},i} = n_i T_{\text{orb}}$ (rejection of the main perturbations)



Division in subsections

Number of data loss > 1 minute	Probability over 120 orbits
1	16%
2	2,5%
3	0.4%
4	0,07%

→ Success probability > 99,5%



Conclusion

- Influence of the observation window
 - Perturbations at any frequency can have a component at the EP frequency
 - Mean perturbations frequencies: adjusted to have minimal projections, but the effects are amplified by the frequencies uncertainty
 - Numerical estimation of the projection rate: compatible with the specification
- Influence of the measurement losses on the projection and rejection rate
 - Numerous very small losses or one loss up to 1 minute: replacement by the mean value of the measurement before and after the interruption
 - Losses > 1 minute: division in separated subsection for the inertial sessions
 - → Acceptable probability of success for the mission
- Possibility of accuracy improvement by using the Hann or Blackman window.